

## Calculation Policy (Published 2022)

At Ivy Lane, the aim of our calculation policy is to ensure all children receive equity of offer. Calculation procedures are taught according to this document so they can be seamlessly built upon year after year, as the child moves through school.

The policy has been taken and adapted to suit from White Rose Maths. We have found their calculation policy to be the one which works for the needs of our children and suits the way in which we teach Maths.

The use of concrete resources and visuals underpins this calculation policy, which is what you would see in an Ivy Lane maths lesson.

The policy goes through:

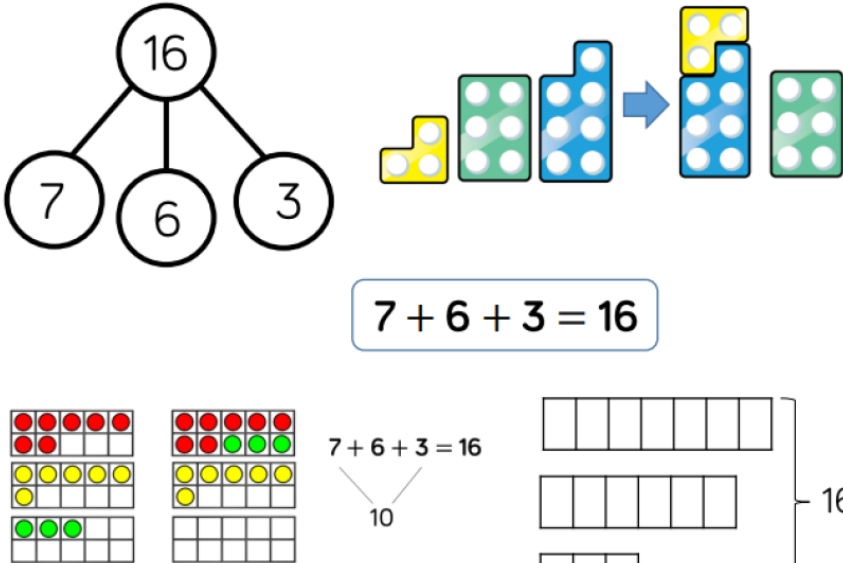
- Addition
- Subtraction
- Multiplication
- Division

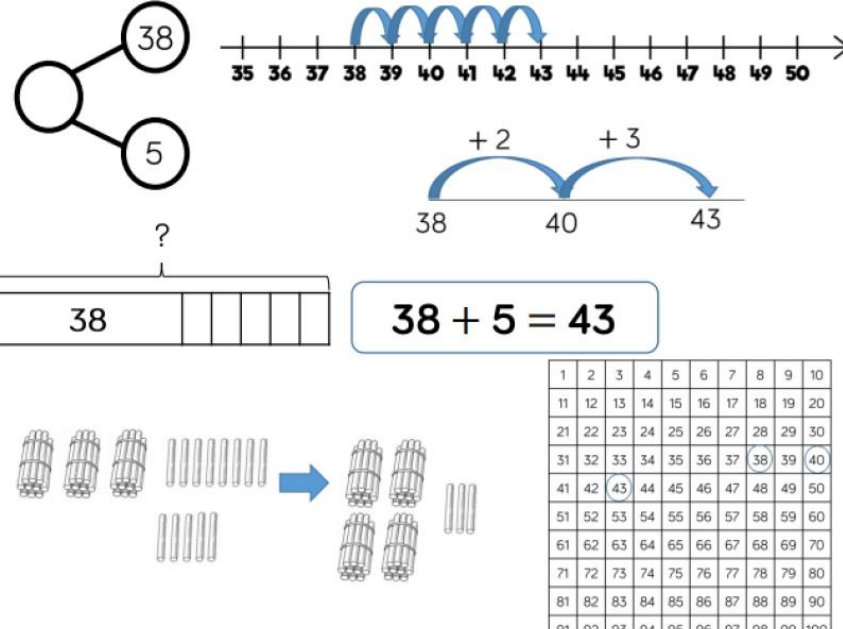
Each operation is broken down into skills for the year group and shows recommended models and visuals to support the teaching of the corresponding concepts alongside.

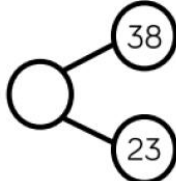
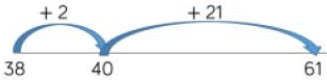
## Addition

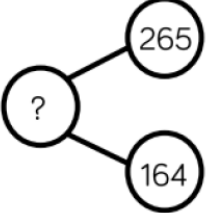
Skill: Add 1-digit numbers within 10	Year: 1
<p><math>4 + 3 = 7</math></p>	<p>When adding numbers to 10, children can explore both aggregation and augmentation.</p> <p>The part-whole model, discrete and continuous bar model, number shapes and ten frame support aggregation.</p> <p>The combination bar model, ten frame, bead string and number track all support augmentation.</p>

Skill: Add 1 and 2-digit numbers to 20	Year: 1/2
	<p>When adding one-digit numbers that cross 10, it is important to highlight the importance of ten ones equalling one ten.</p> <p>Different manipulatives can be used to represent this exchange. Use concrete resources alongside number lines to support children in understanding how to partition their jumps.</p>

Skill: Add three 1-digit numbers	Year: 2
 <p><math>7 + 6 + 3 = 16</math></p>	<p>When adding three 1-digit numbers, children should be encouraged to look for number bonds to 10 or doubles to add the numbers more efficiently.</p> <p>This supports children in their understanding of commutativity.</p> <p>Manipulatives that highlight number bonds to 10 are effective when adding three 1-digit numbers.</p>

Skill: Add 1-digit and 2-digit numbers to 100	Year: 2/3
 <p><math>38 + 5 = 43</math></p>	<p>When adding single digits to a two-digit number, children should be encouraged to count on from the larger number.</p> <p>They should also apply their knowledge of number bonds to add more efficiently e.g. <math>8 + 5 = 13</math> so <math>38 + 5 = 43</math>.</p> <p>Hundred squares and straws can support children to find the number bond to 10.</p>

Skill: Add two 2-digit numbers to 100	Year: 2/3														
<div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;">  </div> <div style="text-align: center;">  </div> </div> <div style="display: flex; justify-content: space-around; align-items: center; margin-top: 10px;"> <div style="border: 1px solid black; padding: 5px; width: 150px;"> <div style="text-align: center; margin-bottom: 5px;">?</div> <table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 50%; border-right: 1px solid black; padding: 5px; text-align: center;">38</td> <td style="width: 50%; padding: 5px; text-align: center;">23</td> </tr> </table> </div> <div style="border: 1px solid black; padding: 10px; background-color: #e6f2ff;"> <math>38 + 23 = 61</math> </div> </div> <div style="display: flex; justify-content: space-around; align-items: center; margin-top: 20px;"> <div style="text-align: center;"> <table border="1" style="border-collapse: collapse; width: 150px;"> <thead> <tr style="background-color: #f2f2f2;"> <th style="padding: 2px 5px;">Tens</th> <th style="padding: 2px 5px;">Ones</th> </tr> </thead> <tbody> <tr> <td style="text-align: center;">    </td> <td style="text-align: center;">     </td> </tr> <tr> <td style="text-align: center;">    </td> <td style="text-align: center;"> </td> </tr> </tbody> </table> </div> <div style="text-align: center;"> <math display="block">\begin{array}{r} 38 \\ + 23 \\ \hline 61 \\ 1 \end{array}</math> </div> <div style="text-align: center;"> <table border="1" style="border-collapse: collapse; width: 150px;"> <thead> <tr style="background-color: #f2f2f2;"> <th style="padding: 2px 5px;">Tens</th> <th style="padding: 2px 5px;">Ones</th> </tr> </thead> <tbody> <tr> <td style="text-align: center;">●●●●</td> <td style="text-align: center;">●●●●●</td> </tr> <tr> <td style="text-align: center;">●●●●</td> <td style="text-align: center;">●●●●●</td> </tr> </tbody> </table> </div> </div>	38	23	Tens	Ones					Tens	Ones	●●●●	●●●●●	●●●●	●●●●●	<p>At this stage, encourage children to use the formal column method when calculating alongside straws, base 10 or place value counters. As numbers become larger, straws become less efficient.</p> <p>Children can also use a blank number line to count on to find the total. Encourage them to jump to multiples of 10 to become more efficient.</p>
38	23														
Tens	Ones														
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Skill: Add numbers with up to 3 digits	Year: 3																						
<div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;">  </div> <div style="text-align: center;"> <div style="margin-bottom: 10px;"> <div style="text-align: center; margin-bottom: 5px;">?</div> <table style="width: 150px; border-collapse: collapse;"> <tr> <td style="width: 50%; border-right: 1px solid black; padding: 5px; text-align: center;">265</td> <td style="width: 50%; padding: 5px; text-align: center;">164</td> </tr> </table> </div> <div style="display: flex; align-items: center;"> <table style="width: 100px; border-collapse: collapse;"> <tr> <td style="border: 1px solid black; padding: 5px; text-align: center;">265</td> </tr> <tr> <td style="border: 1px solid black; padding: 5px; text-align: center;">164</td> </tr> </table> <div style="margin-left: 10px;">}</div> <div style="font-size: 2em;">?</div> </div> </div> </div> <div style="border: 1px solid black; padding: 10px; background-color: #e6f2ff; margin-top: 10px; text-align: center;"> <math>265 + 164 = 429</math> </div> <div style="display: flex; justify-content: space-around; align-items: center; margin-top: 20px;"> <div style="text-align: center;"> <table border="1" style="border-collapse: collapse; width: 200px;"> <thead> <tr style="background-color: #f2f2f2;"> <th style="padding: 2px 5px;">Hundreds</th> <th style="padding: 2px 5px;">Tens</th> <th style="padding: 2px 5px;">Ones</th> </tr> </thead> <tbody> <tr> <td style="text-align: center;">■■■</td> <td style="text-align: center;">     </td> <td style="text-align: center;">     </td> </tr> <tr> <td style="text-align: center;">■</td> <td style="text-align: center;">     </td> <td style="text-align: center;">     </td> </tr> </tbody> </table> </div> <div style="text-align: center;"> <math display="block">\begin{array}{r} 265 \\ + 164 \\ \hline 429 \\ 1 \end{array}</math> </div> <div style="text-align: center;"> <table border="1" style="border-collapse: collapse; width: 200px;"> <thead> <tr style="background-color: #f2f2f2;"> <th style="padding: 2px 5px;">Hundreds</th> <th style="padding: 2px 5px;">Tens</th> <th style="padding: 2px 5px;">Ones</th> </tr> </thead> <tbody> <tr> <td style="text-align: center;">●●●</td> <td style="text-align: center;">●●●●●</td> <td style="text-align: center;">●●●●●</td> </tr> <tr> <td style="text-align: center;">●</td> <td style="text-align: center;">●●●●●</td> <td style="text-align: center;">●●●●●</td> </tr> </tbody> </table> </div> </div>	265	164	265	164	Hundreds	Tens	Ones	■■■			■			Hundreds	Tens	Ones	●●●	●●●●●	●●●●●	●	●●●●●	●●●●●	<p>Base 10 and place value counters are the most effective manipulatives when adding numbers with up to 3 digits.</p> <p>Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.</p> <p>Plain counters on a place value grid can also be used to support learning.</p>
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**Skill: Add numbers with up to 4 digits**
**Year: 4**

	1	3	7	8
+	2	1	4	8
	3	5	2	6
	1		1	

$1,378 + 2,148 = 3,526$

Base 10 and place value counters are the most effective manipulatives when adding numbers with up to 4 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

Plain counters on a place value grid can also be used to support learning.

## Skill: Add numbers with more than 4 digits

Year: 5/6

$$104,328 + 61,731 = 166,059$$

1	0	4	3	2	8
+	6	1	7	3	1
1	6	6	0	5	9

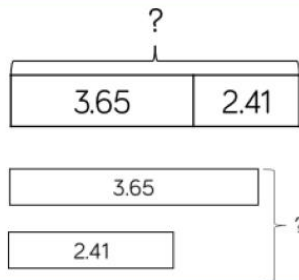
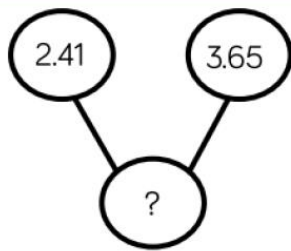
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Place value counters or plain counters on a place value grid are the most effective concrete resources when adding numbers with more than 4 digits.

At this stage, children should be encouraged to work in the abstract, using the column method to add larger numbers efficiently.

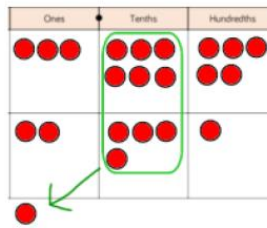
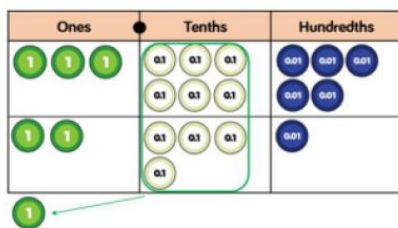
**Skill: Add with up to 3 decimal places**

**Year: 5**



$$\begin{array}{r} 3.65 \\ + 2.41 \\ \hline 6.06 \\ 1 \end{array}$$

$$3.65 + 2.41 = 6.06$$



Place value counters and plain counters on a place value grid are the most effective manipulatives when adding decimals with 1, 2 and then 3 decimal places.

Ensure children have experience of adding decimals with a variety of decimal places. This includes putting this into context when adding money and other measures.

## Subtraction

[illegible]

## Skill: Subtract 1 and 2-digit numbers to 20

Year: 1/2

The figure illustrates various methods for subtracting 6 from 14:

- Number Bond:** A circle containing 14 is connected to two empty circles, one containing 6 and the other empty.
- Number Line:** A horizontal line from 0 to 20. A blue circle is at 14, and a blue circle is at 8. A blue arrow points from 14 to 8, labeled 8.
- Base Ten Blocks:** A ten rod (purple) and a one rod (green) are shown. The ten rod is broken into ten one rods. The ten rod is crossed out with red diagonal lines, and the ten rods are crossed out with red diagonal lines.
- Equation:**  $14 - 6 = 8$  is displayed in a blue box.
- Number Line:** A horizontal line from 0 to 20. A blue circle is at 14, and a blue circle is at 8. A blue arrow points from 14 to 8, labeled 8.
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When subtracting one-digit numbers that cross 10, it is important to highlight the importance of ten ones equalling one ten.

Children should be encouraged to find the number bond to 10 when partitioning the subtracted number. Ten frames, number shapes and number lines are particularly useful for this.

Skill: Subtract 1 and 2-digit numbers to 100	Year: 2								
<p>65</p> <p>28</p> <p>65</p> <p>?</p> <p>28</p> <p><math>65 - 28 = 37</math></p> <table border="1"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td> </td> <td> </td> </tr> </tbody> </table> <p> <math display="block">\begin{array}{r} 65 \\ - 28 \\ \hline 37 \end{array}</math> </p> <table border="1"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td> </td> <td> </td> </tr> </tbody> </table>	Tens	Ones			Tens	Ones			<p>At this stage, encourage children to use the formal column method when calculating alongside straws, base 10 or place value counters. As numbers become larger, straws become less efficient.</p> <p>Children can also use a blank number line to count on to find the difference. Encourage them to jump to multiples of 10 to become more efficient.</p>
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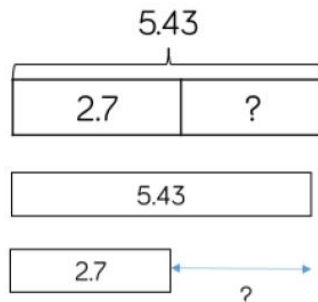
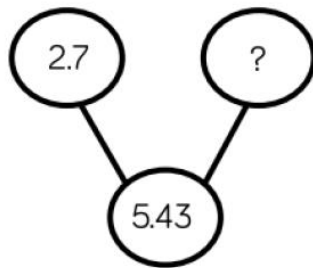
Skill: Subtract numbers with up to 3 digits	Year: 3												
<p>435</p> <p>273</p> <p>?</p> <p>435</p> <p>273</p> <p>?</p> <p><math>435 - 273 = 262</math></p> <table border="1"> <thead> <tr> <th>Hundreds</th> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td> </td> <td> </td> <td> </td> </tr> </tbody> </table> <p> <math display="block">\begin{array}{r} 435 \\ - 273 \\ \hline 262 \end{array}</math> </p> <table border="1"> <thead> <tr> <th>Hundreds</th> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td> </td> <td> </td> <td> </td> </tr> </tbody> </table>	Hundreds	Tens	Ones				Hundreds	Tens	Ones				<p>Base 10 and place value counters are the most effective manipulative when subtracting numbers with up to 3 digits.</p> <p>Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.</p> <p>Plain counters on a place value grid can also be used to support learning.</p>
Hundreds	Tens	Ones											
Hundreds	Tens	Ones											

Skill: Subtract numbers with up to 4 digits	Year: 4																
<div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;"> </div> <div style="text-align: center;"> <math display="block">\begin{array}{r} 4,357 \\ - 2,735 \\ \hline \end{array}</math> </div> <div style="text-align: center;"> <math display="block">\begin{array}{r} 3 \phantom{0} 1 \\ 4357 \\ - 2735 \\ \hline 1622 \end{array}</math> </div> </div> <div style="text-align: center; margin-top: 10px;"> <math display="block">4,357 - 2,735 = 1,622</math> </div> <div style="display: flex; justify-content: space-around; margin-top: 10px;"> <table border="1" style="font-size: 0.8em;"> <tr><th>Thousands</th><th>Hundreds</th><th>Tens</th><th>Ones</th></tr> <tr><td></td><td></td><td></td><td></td></tr> </table> <table border="1" style="font-size: 0.8em;"> <tr><th>Thousands</th><th>Hundreds</th><th>Tens</th><th>Ones</th></tr> <tr><td></td><td></td><td></td><td></td></tr> </table> </div>	Thousands	Hundreds	Tens	Ones					Thousands	Hundreds	Tens	Ones					<p>Base 10 and place value counters are the most effective manipulatives when subtracting numbers with up to 4 digits.</p> <p>Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.</p> <p>Plain counters on a place value grid can also be used to support learning.</p>
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Skill: Subtract numbers with more than 4 digits	Year: 5/6																								
<div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;"> </div> <div style="text-align: center;"> <math display="block">\begin{array}{r} 294,382 \\ - 182,501 \\ \hline \end{array}</math> </div> </div> <div style="text-align: center; margin-top: 10px;"> <math display="block">294,382 - 182,501 = 111,881</math> </div> <div style="display: flex; justify-content: space-around; margin-top: 10px;"> <table border="1" style="font-size: 0.8em;"> <tr><th>HTh</th><th>TTh</th><th>Th</th><th>H</th><th>T</th><th>O</th></tr> <tr><td></td><td></td><td></td><td></td><td></td><td></td></tr> </table> <table border="1" style="font-size: 0.8em;"> <tr><th>HTh</th><th>TTh</th><th>Th</th><th>H</th><th>T</th><th>O</th></tr> <tr><td></td><td></td><td></td><td></td><td></td><td></td></tr> </table> </div>	HTh	TTh	Th	H	T	O							HTh	TTh	Th	H	T	O							<p>Place value counters or plain counters on a place value grid are the most effective concrete resource when subtracting numbers with more than 4 digits.</p> <p>At this stage, children should be encouraged to work in the abstract, using column method to subtract larger numbers efficiently.</p>
HTh	TTh	Th	H	T	O																				
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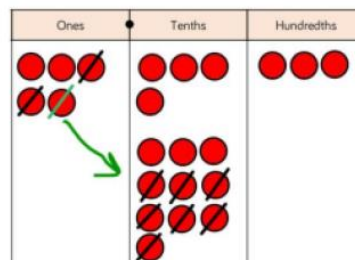
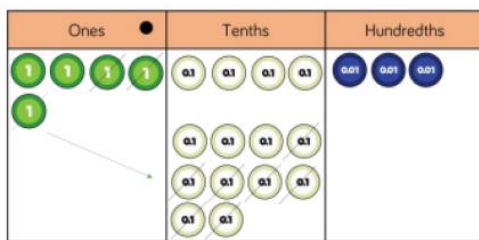
# Skill: Subtract with up to 3 decimal places

Year: 5



$$\begin{array}{r} 4 \quad 1 \\ \cancel{5}.43 \\ - 2.7 \\ \hline 2.73 \end{array}$$

$$5.43 - 2.7 = 2.73$$



Place value counters and plain counters on a place value grid are the most effective manipulative when subtracting decimals with 1, 2 and then 3 decimal places.

Ensure children have experience of subtracting decimals with a variety of decimal places. This includes putting this into context when subtracting money and other measures.

## Multiplication

Our calculation policy for multiplication starts with a breakdown of times tables; what should be taught when and what that teaching should look like. To enhance the learning of multiplications we will also teach the use of the inverse operation to find known facts through the use of our Math's Passport targets.

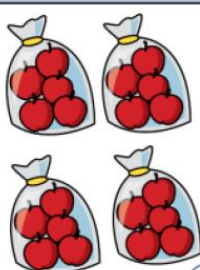
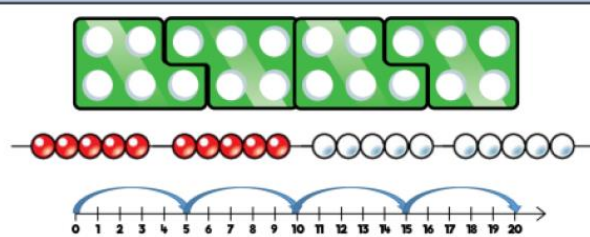
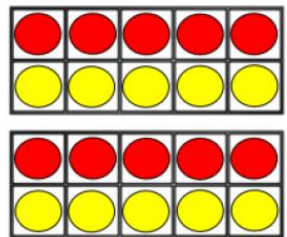
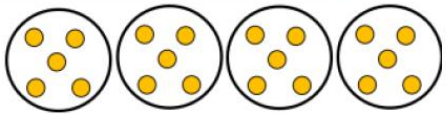
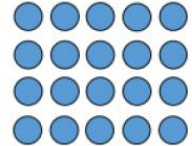
During the Summer Term, the children in Year 4 sit the Multiplication Tables Check in line with the Government's assessment framework.

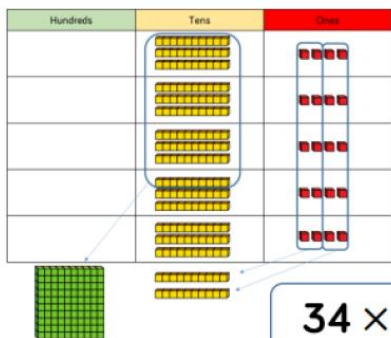
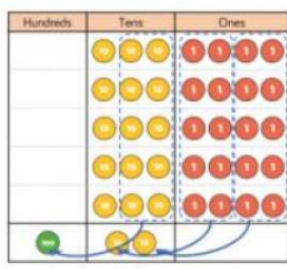
Times tables continue to be recalled and tested throughout Years 5 and 6.

Skill	Year	Representations and models	
Recall and use multiplication and division facts for the 2-times table	2	Bar model Number shapes Counters Money	Ten frames Bead strings Number lines Everyday objects
Recall and use multiplication and division facts for the 5-times table	2	Bar model Number shapes Counters Money	Ten frames Bead strings Number lines Everyday objects
Recall and use multiplication and division facts for the 10-times table	2	Hundred square Number shapes Counters Money	Ten frames Bead strings Number lines Base 10

Skill	Year	Representations and models	
Recall and use multiplication and division facts for the 3-times table	3	Hundred square Number shapes Counters	Bead strings Number lines Everyday objects
Recall and use multiplication and division facts for the 4-times table	3	Hundred square Number shapes Counters	Bead strings Number lines Everyday objects
Recall and use multiplication and division facts for the 8-times table	3	Hundred square Number shapes	Bead strings Number tracks Everyday objects
Recall and use multiplication and division facts for the 6-times table	4	Hundred square Number shapes	Bead strings Number tracks Everyday objects

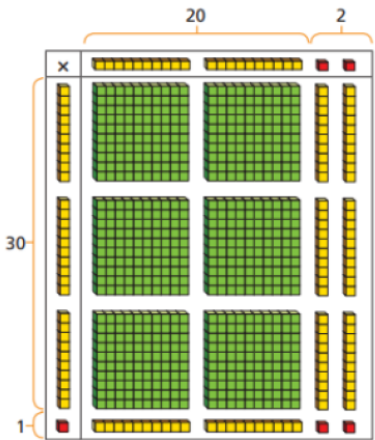
Skill	Year	Representations and models	
Recall and use multiplication and division facts for the 7-times table	4	Hundred square Number shapes	Bead strings Number lines
Recall and use multiplication and division facts for the 9-times table	4	Hundred square Number shapes	Bead strings Number lines
Recall and use multiplication and division facts for the 11-times table	4	Hundred square Base 10	Place value counters Number lines
Recall and use multiplication and division facts for the 12-times table	4	Hundred square Base 10	Place value counters Number lines

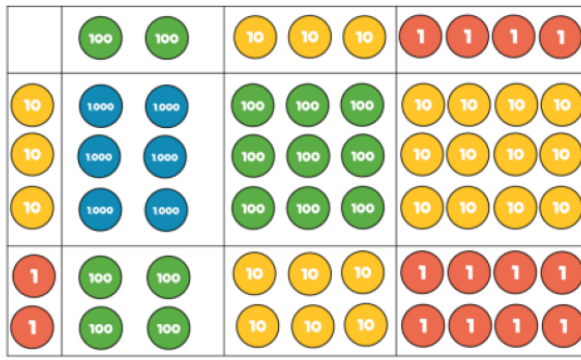
Skill: Solve 1-step problems using multiplication	Year: 1/2
<div style="display: flex; justify-content: space-around; align-items: center;">   </div> <div style="border: 1px solid black; border-radius: 10px; padding: 10px; margin: 10px auto; width: fit-content; text-align: center;"> <p>One bag holds 5 apples. How many apples do 4 bags hold?</p> </div> <div style="display: flex; justify-content: space-around; align-items: center; margin-top: 20px;">  <div style="text-align: center;">     </div> <div style="text-align: left;"> <math>5 + 5 + 5 + 5 = 20</math>  <math>4 \times 5 = 20</math>  <math>5 \times 4 = 20</math> </div> </div>	<p>Children represent multiplication as repeated addition in many different ways.</p> <p>In Year 1, children use concrete and pictorial representations to solve problems. They are not expected to record multiplication formally.</p> <p>In Year 2, children are introduced to the multiplication symbol.</p>

Skill: Multiply 2-digit numbers by 1-digit numbers	Year: 3/4																												
<div style="display: flex; justify-content: space-around; align-items: center;">  <div style="text-align: center;"> <math>34 \times 5 = 170</math> </div> </div> <div style="display: flex; justify-content: space-around; align-items: center; margin-top: 20px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <thead> <tr><th></th><th>H</th><th>T</th><th>O</th></tr> </thead> <tbody> <tr><td></td><td></td><td>3</td><td>4</td></tr> <tr><td>x</td><td></td><td></td><td>5</td></tr> <tr><td colspan="4" style="border-top: 1px solid black;"></td></tr> <tr><td>+</td><td>1</td><td>7</td><td>0</td></tr> <tr><td colspan="4" style="border-top: 1px solid black;"></td></tr> <tr><td></td><td>1</td><td>7</td><td>0</td></tr> </tbody> </table>  </div>		H	T	O			3	4	x			5					+	1	7	0						1	7	0	<p>Teachers may decide to first look at the expanded column method before moving on to the short multiplication method.</p> <p>The place value counters should be used to support the understanding of the method rather than supporting the multiplication, as children should use times table knowledge.</p>
	H	T	O																										
		3	4																										
x			5																										
+	1	7	0																										
	1	7	0																										

Skill: Multiply 3-digit numbers by 1-digit numbers				Year: 3/4																			
<div style="display: flex; justify-content: space-around; font-size: 0.8em;"> <span>Hundreds</span> <span>Tens</span> <span>Ones</span> </div>	<table border="1" style="border-collapse: collapse; margin: auto;"> <tr><td></td><td>H</td><td>T</td><td>O</td></tr> <tr><td></td><td>2</td><td>4</td><td>5</td></tr> <tr><td>x</td><td></td><td></td><td>4</td></tr> <tr style="border-top: 1px solid black;"><td></td><td>9</td><td>8</td><td>0</td></tr> <tr><td></td><td>1</td><td>2</td><td></td></tr> </table>		H	T	O		2	4	5	x			4		9	8	0		1	2		<p>When moving to 3-digit by 1-digit multiplication, encourage children to move towards the short, formal written method. Base 10 and place value counters continue to support the understanding of the written method. Limit the number of exchanges needed in the questions and move children away from resources when multiplying larger numbers.</p>	
	H	T	O																				
	2	4	5																				
x			4																				
	9	8	0																				
	1	2																					
<div style="border: 1px solid black; border-radius: 10px; padding: 10px; display: inline-block;"> <math>245 \times 4 = 980</math> </div>																							



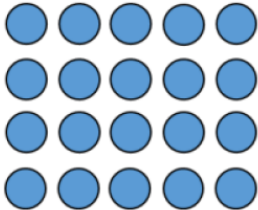
Skill: Multiply 4-digit numbers by 1-digit numbers				Year: 5																								
<div style="display: flex; justify-content: space-around; font-size: 0.8em;"> <span>Thousands</span> <span>Hundreds</span> <span>Tens</span> <span>Ones</span> </div>	<p>When multiplying 4-digit numbers, place value counters are the best manipulative to use to support children in their understanding of the formal written method. If children are multiplying larger numbers and struggling with their times tables, encourage the use of multiplication grids so children can focus on the use of the written method.</p>																											
<div style="border: 1px solid black; border-radius: 10px; padding: 10px; display: inline-block;"> <math>1,826 \times 3 = 5,478</math> </div>																												
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	5	4	7	8																								
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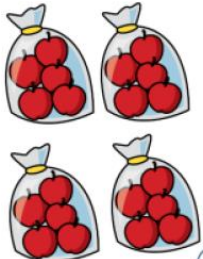
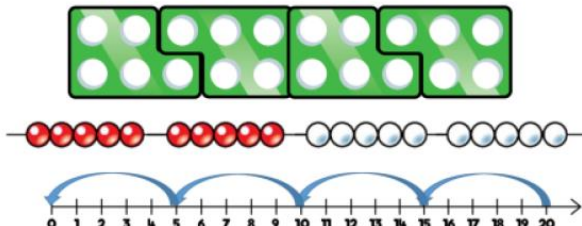
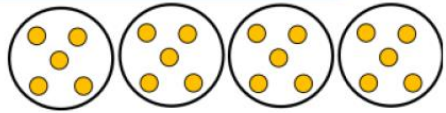
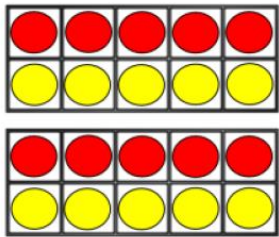
Skill: Multiply 2-digit numbers by 2-digit numbers	Year: 5																																																										
<div style="display: flex; align-items: center;">  <div style="margin-left: 20px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td></td><td>10</td><td>10</td><td>1</td><td>1</td></tr> <tr><td>10</td><td>100</td><td>100</td><td>10</td><td>10</td></tr> <tr><td>10</td><td>100</td><td>100</td><td>10</td><td>10</td></tr> <tr><td>10</td><td>100</td><td>100</td><td>10</td><td>10</td></tr> <tr><td>1</td><td>10</td><td>10</td><td>1</td><td>1</td></tr> </table> </div> </div> <div style="margin-top: 10px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td>×</td><td>20</td><td>2</td></tr> <tr><td>30</td><td>600</td><td>60</td></tr> <tr><td>1</td><td>20</td><td>2</td></tr> </table> </div> <div style="margin-top: 10px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td></td><td>H</td><td>T</td><td>O</td></tr> <tr><td></td><td></td><td>2</td><td>2</td></tr> <tr><td>×</td><td></td><td>3</td><td>1</td></tr> <tr><td></td><td></td><td>2</td><td>2</td></tr> <tr><td></td><td>6</td><td>6</td><td>0</td></tr> <tr><td></td><td>6</td><td>8</td><td>2</td></tr> </table> </div> <div style="margin-top: 20px; border: 1px solid black; padding: 5px; display: inline-block;"> <math>22 \times 31 = 682</math> </div>		10	10	1	1	10	100	100	10	10	10	100	100	10	10	10	100	100	10	10	1	10	10	1	1	×	20	2	30	600	60	1	20	2		H	T	O			2	2	×		3	1			2	2		6	6	0		6	8	2	<p>When multiplying a multi-digit number by 2-digits, use the area model to help children understand the size of the numbers they are using. This links to finding the area of a rectangle by finding the space covered by the Base 10.</p> <p>The grid method matches the area model as an initial written method before moving on to the formal written multiplication method.</p>
	10	10	1	1																																																							
10	100	100	10	10																																																							
10	100	100	10	10																																																							
10	100	100	10	10																																																							
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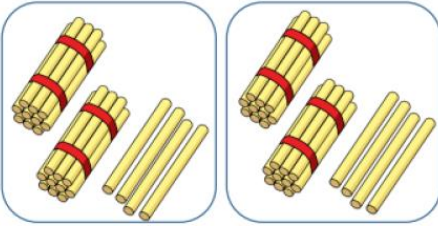
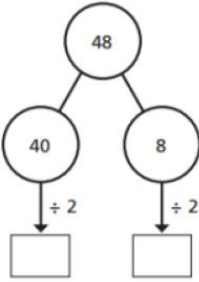
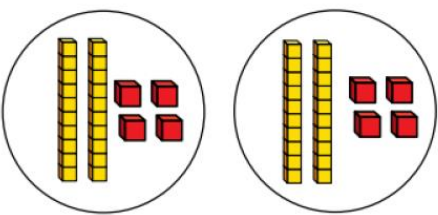
Skill: Multiply 3-digit numbers by 2-digit numbers	Year: 5																																																																																																								
<div style="display: flex; align-items: center;">  <div style="margin-left: 20px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td></td><td>100</td><td>100</td><td>10</td><td>10</td><td>10</td><td>1</td><td>1</td><td>1</td><td>1</td></tr> <tr><td>10</td><td>1000</td><td>1000</td><td>100</td><td>100</td><td>100</td><td>10</td><td>10</td><td>10</td><td>10</td></tr> <tr><td>10</td><td>1000</td><td>1000</td><td>100</td><td>100</td><td>100</td><td>10</td><td>10</td><td>10</td><td>10</td></tr> <tr><td>10</td><td>1000</td><td>1000</td><td>100</td><td>100</td><td>100</td><td>10</td><td>10</td><td>10</td><td>10</td></tr> <tr><td>1</td><td>100</td><td>100</td><td>10</td><td>10</td><td>10</td><td>1</td><td>1</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>100</td><td>100</td><td>10</td><td>10</td><td>10</td><td>1</td><td>1</td><td>1</td><td>1</td></tr> </table> </div> </div> <div style="margin-top: 10px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td></td><td>Th</td><td>H</td><td>T</td><td>O</td></tr> <tr><td></td><td></td><td>2</td><td>3</td><td>4</td></tr> <tr><td>×</td><td></td><td></td><td>3</td><td>2</td></tr> <tr><td></td><td></td><td>4</td><td>6</td><td>8</td></tr> <tr><td>1</td><td>7</td><td>1</td><td>0</td><td>2</td><td>0</td></tr> <tr><td>7</td><td></td><td>4</td><td>8</td><td>8</td><td></td></tr> </table> </div> <div style="margin-top: 20px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td>×</td><td>200</td><td>30</td><td>4</td></tr> <tr><td>30</td><td>6,000</td><td>900</td><td>120</td></tr> <tr><td>2</td><td>400</td><td>60</td><td>8</td></tr> </table> </div> <div style="margin-top: 20px; border: 1px solid black; padding: 5px; display: inline-block;"> <math>234 \times 32 = 7,488</math> </div>		100	100	10	10	10	1	1	1	1	10	1000	1000	100	100	100	10	10	10	10	10	1000	1000	100	100	100	10	10	10	10	10	1000	1000	100	100	100	10	10	10	10	1	100	100	10	10	10	1	1	1	1	1	100	100	10	10	10	1	1	1	1		Th	H	T	O			2	3	4	×			3	2			4	6	8	1	7	1	0	2	0	7		4	8	8		×	200	30	4	30	6,000	900	120	2	400	60	8	<p>Children can continue to use the area model when multiplying 3-digits by 2-digits. Place value counters become more efficient to use but Base 10 can be used to highlight the size of numbers.</p> <p>Encourage children to move towards the formal written method, seeing the links with the grid method.</p>
	100	100	10	10	10	1	1	1	1																																																																																																
10	1000	1000	100	100	100	10	10	10	10																																																																																																
10	1000	1000	100	100	100	10	10	10	10																																																																																																
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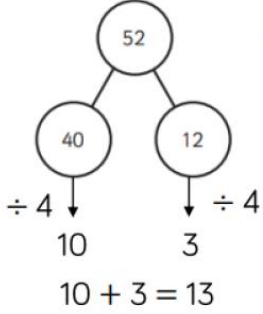

Skill: Multiply 4-digit numbers by 2-digit numbers	Year: 5/6																																								
<table><tr><th>TTh</th><th>Th</th><th>H</th><th>T</th><th>O</th></tr><tr><td></td><td>2</td><td>7</td><td>3</td><td>9</td></tr><tr><td>×</td><td></td><td></td><td>2</td><td>8</td></tr><tr><td>2</td><td>1</td><td>9</td><td>1</td><td>2</td></tr><tr><td>2</td><td>5</td><td>3</td><td>7</td><td></td></tr><tr><td>5</td><td>4</td><td>7</td><td>8</td><td>0</td></tr><tr><td>1</td><td></td><td>1</td><td></td><td></td></tr><tr><td>7</td><td>6</td><td>6</td><td>9</td><td>2</td></tr></table> <p>1</p> <div>2,739 × 28 = 76,692</div>	TTh	Th	H	T	O		2	7	3	9	×			2	8	2	1	9	1	2	2	5	3	7		5	4	7	8	0	1		1			7	6	6	9	2	<p>When multiplying 4-digits by 2-digits, children should be confident in the written method.</p> <p>If they are still struggling with times tables, provide multiplication grids to support when they are focusing on the use of the method.</p> <p>Consider where exchanged digits are placed and make sure this is consistent.</p>
TTh	Th	H	T	O																																					
	2	7	3	9																																					
×			2	8																																					
2	1	9	1	2																																					
2	5	3	7																																						
5	4	7	8	0																																					
1		1																																							
7	6	6	9	2																																					


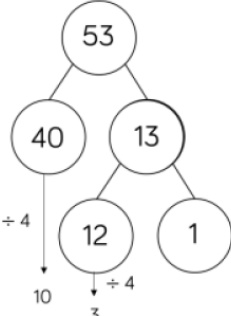

Division

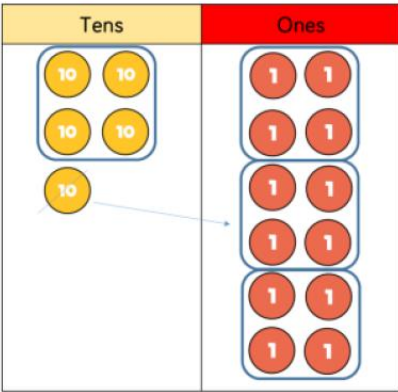
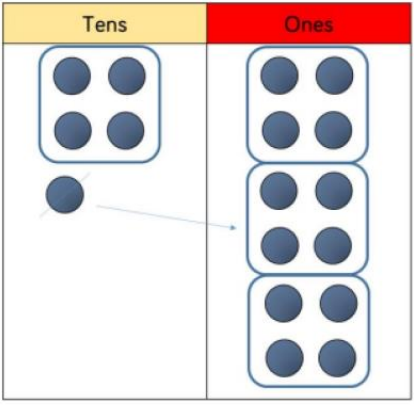
Skill: Solve 1-step problems using multiplication (sharing)	Year: 1/2
<div><div>20</div><div><div>?</div><div>?</div><div>?</div><div>?</div><div>?</div></div></div> <div><div>There are 20 apples altogether. They are shared equally between 5 bags. How many apples are in each bag?</div><div><div><math>20 \div 5 = 4</math></div></div></div>	<p>Children solve problems by sharing amounts into equal groups.</p> <p>In Year 1, children use concrete and pictorial representations to solve problems. They are not expected to record division formally.</p> <p>In Year 2, children are introduced to the division symbol.</p>

Skill: Solve 1-step problems using division (grouping)	Year: 1/2
<div><div><div>0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20</div></div></div> <div><div>There are 20 apples altogether. They are put in bags of 5. How many bags are there?</div><div><div><math>20 \div 5 = 4</math></div></div></div>	<p>Children solve problems by grouping and counting the number of groups. Grouping encourages children to count in multiples and links to repeated subtraction on a number line. They can use concrete representations in fixed groups such as number shapes which helps to show the link between multiplication and division.</p>

Skill: Divide 2-digits by 1-digit (sharing with no exchange)	Year: 1/2						
<div style="display: flex; justify-content: space-around; align-items: flex-start;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <thead> <tr style="background-color: #fff9c4;"> <th style="padding: 2px 10px;">Tens</th> <th style="padding: 2px 10px;">Ones</th> </tr> </thead> <tbody> <tr> <td style="padding: 2px 10px;">10 10</td> <td style="padding: 2px 10px;">1 1 1 1</td> </tr> <tr> <td style="padding: 2px 10px;">10 10</td> <td style="padding: 2px 10px;">1 1 1 1</td> </tr> </tbody> </table> <div style="text-align: center;">  </div> </div> <div style="text-align: center; margin: 20px 0;"> <div style="display: flex; align-items: center; justify-content: center;"> <div style="text-align: center;">  <div style="border: 1px solid black; border-radius: 10px; padding: 5px; margin: 0 10px;"> <math>48 \div 2 = 24</math> </div> <div style="text-align: center;">  </div> </div> </div> </div>	Tens	Ones	10 10	1 1 1 1	10 10	1 1 1 1	<p>When dividing larger numbers, children can use manipulatives that allow them to partition into tens and ones.</p> <p>Straws, Base 10 and place value counters can all be used to share numbers into equal groups.</p> <p>Part-whole models can provide children with a clear written method that matches the concrete representation.</p>
Tens	Ones						
10 10	1 1 1 1						
10 10	1 1 1 1						

Skill: Divide 2-digits by 1-digit (sharing with exchange)	Year: 3/4														
<div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;">  </div> <table border="1" style="border-collapse: collapse; text-align: center;"> <thead> <tr style="background-color: #fff9c4;"> <th style="padding: 2px 10px;">Tens</th> <th style="padding: 2px 10px;">Ones</th> </tr> </thead> <tbody> <tr><td style="padding: 2px 10px;">10</td><td style="padding: 2px 10px;">2</td></tr> <tr><td style="padding: 2px 10px;">10</td><td style="padding: 2px 10px;">2</td></tr> <tr><td style="padding: 2px 10px;">10</td><td style="padding: 2px 10px;">2</td></tr> <tr><td style="padding: 2px 10px;">10</td><td style="padding: 2px 10px;">2</td></tr> </tbody> </table> <div style="text-align: center;"> <div style="margin-bottom: 5px;">52</div> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td style="width: 25px; height: 25px;">?</td><td style="width: 25px; height: 25px;">?</td><td style="width: 25px; height: 25px;">?</td><td style="width: 25px; height: 25px;">?</td></tr> </table> </div> </div> <div style="text-align: center; margin: 20px 0;"> <div style="display: flex; align-items: center; justify-content: center;"> <div style="text-align: center;">  <div style="border: 1px solid black; border-radius: 10px; padding: 5px; margin: 0 10px;"> <math>52 \div 4 = 13</math> </div> <div style="text-align: center;">  </div> </div> </div> </div>	Tens	Ones	10	2	10	2	10	2	10	2	?	?	?	?	<p>When dividing numbers involving an exchange, children can use Base 10 and place value counters to exchange one ten for ten ones.</p> <p>Children should start with the equipment outside the place value grid before sharing the tens and ones equally between the rows.</p> <p>Flexible partitioning in a part-whole model supports this method.</p>
Tens	Ones														
10	2														
10	2														
10	2														
10	2														
?	?	?	?												

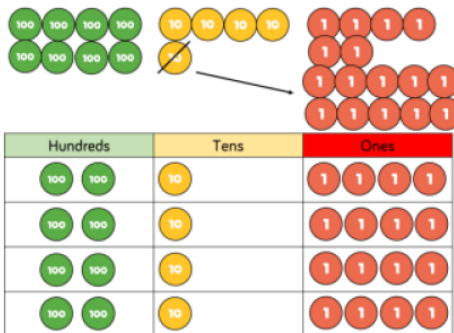
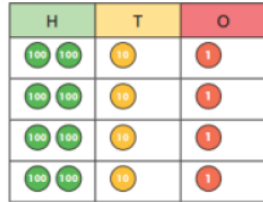
Skill: Divide 2-digits by 1-digit (sharing with remainders)	Year: 3/4
 <div style="text-align: center; margin-top: 10px;"> <math>53 \div 4 = 13 \text{ r}1</math> </div>  	<p>When dividing numbers with remainders, children can use Base 10 and place value counters to exchange one ten for ten ones.</p> <p>Starting with the equipment outside the place value grid will highlight remainders, as they will be left outside the grid once the equal groups have been made.</p> <p>Flexible partitioning in a part-whole model supports this method.</p>

Skill: Divide 2-digits by 1-digit (grouping)	Year: 4/5
 <div style="text-align: center; margin-top: 10px;"> <math>52 \div 4 = 13</math> </div> 	<p>When using the short division method, children use grouping. Starting with the largest place value, they group by the divisor.</p> <p>Language is important here. Children should consider 'How many groups of 4 tens can we make?' and 'How many groups of 4 ones can we make?'</p> <p>Remainders can also be seen as they are left ungrouped.</p>

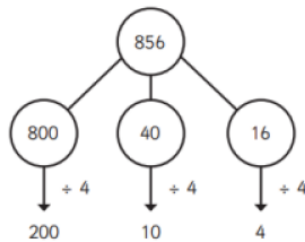
Skill: Divide 3-digits by 1-digit (sharing)

Year: 4

$$844 \div 4 = 211$$



$$844 \div 4 = 211$$



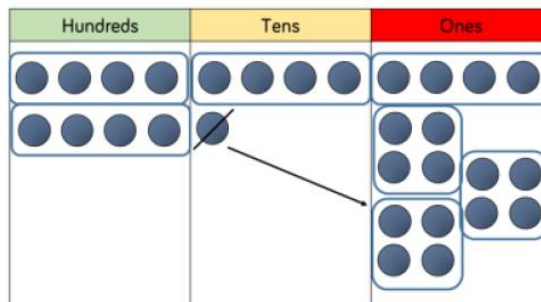
Children can continue to use place value counters to share 3-digit numbers into equal groups. Children should start with the equipment outside the place value grid before sharing the hundreds, tens and ones equally between the rows. This method can also help to highlight remainders. Flexible partitioning in a part-whole model supports this method.

Skill: Divide 3-digits by 1-digit (grouping)

Year: 5



$$856 \div 4 = 214$$



Children can continue to use grouping to support their understanding of short division when dividing a 3-digit number by a 1-digit number.

Place value counters or plain counters can be used on a place value grid to support this understanding. Children can also draw their own counters and group them through a more pictorial method.

Skill: Divide 4-digits by 1-digit (grouping)	Year: 5																																										
<div style="display: flex; align-items: center; justify-content: center; margin-bottom: 20px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <thead> <tr style="background-color: #d9e1f2;"> <th style="width: 12.5%;">Th</th> <th style="width: 12.5%;">H</th> <th style="width: 12.5%;">T</th> <th style="width: 12.5%;">O</th> </tr> </thead> <tbody> <tr> <td><div>1,000</div><div>1,000</div></td> <td><div>100</div><div>100</div></td> <td><div>10</div><div>10</div></td> <td><div>1</div><div>1</div></td> </tr> <tr> <td><div>1,000</div><div>1,000</div></td> <td><div>100</div><div>100</div></td> <td><div>10</div> → <div>1</div></td> <td><div>1</div><div>1</div></td> </tr> <tr> <td><div>1,000</div><div>1,000</div></td> <td><div>100</div> → <div>10</div></td> <td><div>10</div><div>10</div></td> <td><div>1</div><div>1</div></td> </tr> <tr> <td><div>1,000</div><div>1,000</div></td> <td></td> <td><div>10</div><div>10</div></td> <td><div>1</div><div>1</div></td> </tr> <tr> <td></td> <td></td> <td><div>10</div><div>10</div></td> <td><div>1</div><div>1</div></td> </tr> <tr> <td></td> <td></td> <td><div>10</div><div>10</div></td> <td><div>1</div><div>1</div></td> </tr> <tr> <td></td> <td></td> <td><div>10</div><div>10</div></td> <td><div>1</div><div>1</div></td> </tr> </tbody> </table> <div style="margin-left: 20px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td></td><td>4</td><td>2</td><td>6</td><td>6</td></tr> <tr><td>2</td><td>8</td><td>5</td><td>13</td><td>12</td></tr> </table> </div> </div> <div style="border: 1px solid black; border-radius: 10px; padding: 5px; width: fit-content; margin: 0 auto;"> <math>8,532 \div 2 = 4,266</math> </div>	Th	H	T	O	<div>1,000</div> <div>1,000</div>	<div>100</div> <div>100</div>	<div>10</div> <div>10</div>	<div>1</div> <div>1</div>	<div>1,000</div> <div>1,000</div>	<div>100</div> <div>100</div>	<div>10</div> → <div>1</div>	<div>1</div> <div>1</div>	<div>1,000</div> <div>1,000</div>	<div>100</div> → <div>10</div>	<div>10</div> <div>10</div>	<div>1</div> <div>1</div>	<div>1,000</div> <div>1,000</div>		<div>10</div> <div>10</div>	<div>1</div> <div>1</div>			<div>10</div> <div>10</div>	<div>1</div> <div>1</div>			<div>10</div> <div>10</div>	<div>1</div> <div>1</div>			<div>10</div> <div>10</div>	<div>1</div> <div>1</div>		4	2	6	6	2	8	5	13	12	<p>Place value counters or plain counters can be used on a place value grid to support children to divide 4-digits by 1-digit. Children can also draw their own counters and group them through a more pictorial method.</p> <p>Children should be encouraged to move away from the concrete and pictorial when dividing numbers with multiple exchanges.</p>
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Skill: Divide multi digits by 2-digits (short division)	Year: 6																														
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# Skill: Divide multi-digits by 2-digits (long division)

Year: 6

		0	3	6
1	2	4	3	2
	-	3	6	0
			7	2
	-		7	2
				0

(x30)  
 $12 \times 1 = 12$   
 $12 \times 2 = 24$   
 $12 \times 3 = 36$   
 $12 \times 4 = 48$   
 $12 \times 5 = 60$   
 $12 \times 6 = 72$   
 $12 \times 7 = 84$   
 $12 \times 8 = 96$   
 $12 \times 9 = 108$   
 $12 \times 10 = 120$

$$432 \div 12 = 36$$

Children can also divide by 2-digit numbers using long division.

Children can write out multiples to support their calculations with larger remainders.

Children will also solve problems with remainders where the quotient can be rounded as appropriate.

$$7,335 \div 15 = 489$$

	0	4	8	9
15	7	3	3	5
-	6	0	0	0
	1	3	3	5
-	1	2	0	0
		1	3	5
-		1	3	5
				0

(x400)  
 $1 \times 15 = 15$   
 $2 \times 15 = 30$   
 $3 \times 15 = 45$   
 $4 \times 15 = 60$   
 $5 \times 15 = 75$   
 $10 \times 15 = 150$

# Skill: Divide multi digits by 2-digits (long division)

Year: 6

$$372 \div 15 = 24 \text{ r}12$$

		2	4	r	1	2
1	5	3	7	2		
	-	3	0	0		
		7	2			
	-	6	0			
		1	2			

$1 \times 15 = 15$   
 $2 \times 15 = 30$   
 $3 \times 15 = 45$   
 $4 \times 15 = 60$   
 $5 \times 15 = 75$   
 $10 \times 15 = 150$

When a remainder is left at the end of a calculation, children can either leave it as a remainder or convert it to a fraction. This will depend on the context of the question.

Children can also answer questions where the quotient needs to be rounded according to the context.

		2	4	$\frac{4}{5}$
1	5	3	7	2
	-	3	0	0
		7	2	
	-	6	0	
		1	2	

$$372 \div 15 = 24 \frac{4}{5}$$